# Universidade Federal de Minas Gerais - Programa de Pós-Graduação em Engenharia Elétrica 

# EEE945 - INTRODUÇÃO AOS PROCESSOS ESTOCÁSTICOS 

## HOMEWORK 4

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Problem 1. Define a hidden Markov model of your choice with a $6 \times 6$ transition matrix $A$ and a $6 \times 4$ observation matrix $B$. Simulate this model in order to obtain an observation sequence $Y_{0}^{100}$. Apply the forward-backward algorithm, Viterbi's algorithm and the Baum-Welch algorithm to this data set. In your solution, compare the filtered states with the real ones known from simulation.

Problem 2. Consider the Markov chain on $\mathbb{R}$ given by:

$$
X_{n+1}=a X_{n}+W_{n}
$$

where $a<1$ and $\left\{W_{n}\right\}_{n=0}^{\infty}$ are i.i.d. with $W_{n} \sim \gamma(w), \gamma(w)>0$ on $(-1,1)$ and $\mathrm{E}\left[W_{n}^{k}\right]<\infty$. Using the Foster-Lyapunov theorem, show that $X_{n}$ is positive recurrent and that its $k$-th moment is bounded.

